Exploiting Azimuthal Variance Of Scatterers
For Multiple Look SAR Recognition

Bir Bhanu and Grinnell Jones III
Center for Research in Intelligent Systems
University of California, Riverside, California 92521 USA

ABSTRACT

The focus of this paper is optimizing the recognition of vehicles in Synthetic Aperture Radar (SAR) imagery using multiple SAR recognizers at different look angles. The variance of SAR scattering center locations with target azimuth leads to recognition system results at different azimuths that are independent, even for small azimuth deltas. Extensive experimental recognition results are presented in terms of receiver operating characteristic (ROC) curves to show the effects of multiple look angles on recognition performance for MSTAR vehicle targets with configuration variants, articulation, and occlusion.

Keywords: automatic target recognition, synthetic aperture radar, multiple recognizers, recognizing occluded objects, articulated object recognition, recognizing configuration variants

1. INTRODUCTION

In this paper we are concerned with optimizing the recognition of vehicles in Synthetic Aperture Radar (SAR) imagery by using multiple SAR recognizers at different look angles. The recognition system starts with real SAR chips (at one foot resolution) of actual military vehicles from the MSTAR public data\(^4\) and ends with the identification of a specific vehicle type (e.g., a T72 tank). A major challenge is that the vehicles can have significant external configuration variants (fuel barrels, searchlights, etc.), they can be in articulated configurations (such as a tank with its turret rotated), or they can be partially occluded. This paper extends our previous work on SAR recognition\(^1,4,5,6\) to multiple recognizers at different look angles. It takes a principled approach to multiple look angle SAR recognition and answers two fundamental questions: 1) what should the next view angle be? and 2) how to integrate the results? We know of no prior published work on SAR recognition at multiple look angles.

The key contributions of this paper are:

1. Uses the fundamental azimuthal variance of SAR scatterer locations as the basis for a principled approach to multiple look angle SAR recognition.
2. Demonstrates that SAR recognition results at different azimuths are independent, even for small azimuths, such as one degree.
3. Shows that decision level fusion of two observations at different look angles can substantially increase SAR recognition performance.
4. Shows that these results apply to target configuration variants, articulated objects and occluded objects.

The remainder of this paper is organized as follows: the next section demonstrates the azimuthal variance of SAR scattering center locations; Section 3 gives a description of the SAR recognition system; Section 4 demonstrates that multiple look angle SAR recognition results are independent; Section 5 gives experimental results for multiple look angle SAR recognition with configuration variant, articulated and occluded objects; and finally Section 6 has conclusions and suggests future work.

Further author information -
Email: {bhanu, or grinnell} @cris.ucr.edu
URL: http://cris.ucr.edu
2. AZIMUTHAL VARIANCE of SAR SCATTERERS

Figure 1 shows an example of a typical T72 tank SAR target chip image (at 66° azimuth) and the associated region of interest (ROI) with the locations of the SAR scattering centers superimposed. The typical rigid body rotational transformations for viewing objects in the visual world do not apply much for the specular radar reflections of SAR images, where we use the locations of SAR scattering centers (determined from local peaks in the radar return) as features. This is because, as we have previously shown, a significant number of features do not typically persist over a few degrees of rotation.¹

Because the radar depression angle is generally known, the significant unknown target rotation is (360°) in azimuth. Azimuth persistence or invariance can be expressed in terms of the percentage of scattering center locations that are unchanged over a certain span of azimuth angles. It can be measured (for some base azimuth θ₀) by rotating the pixel locations of the scattering centers from an image at azimuth θ₀ by an angle Δθ and comparing the resulting range and cross-range locations with the scatterer locations from an image of the same object at azimuth θ₀ + Δθ. More precisely, because the images are in the radar slant plane, we actually project from the slant plane to the ground plane, rotate in the ground plane and project back to the slant plane. Because the objects in the chips are not registered, we calculate the azimuth invariance as the maximum number of corresponding scattering centers (whose locations match within a given tolerance) for the optimum integer pixel translation. This method of registration by finding the translation that yields the maximum number of correspondences has the limitation that for very small or no actual invariance it may find some false correspondences and report a slightly higher invariance than in fact exists. To determine scattering center locations that persist over a span of angles, there is an additional constraint that for a matching scattering center to 'persist' at the kth span Δθₖ, it must have been a persistent scattering center at all smaller spans Δθⱼ, where 0 ≤ j < k. Averaging the results of these persistent scattering center locations over 360 base azimuths gives the mean azimuth invariance of the object.

Figure 2 shows an example of the mean scatterer location invariance (for the 40 strongest scatterers) as a function of azimuth angle span using T72 tank serial number (#)132, with various definitions of persistence. In the 'exact match' cases the centroid of the rotated scatterer pixel from the image at θ₀ azimuth is within the pixel boundaries of a corresponding scatterer in the image at θ₀ + Δθ. In the 'within 1 pixel' cases, the scatterer location is allowed to move into one of the 8 adjacent pixel locations. Note that for a 1° azimuth span, although only 20% of the scatterer locations are invariant for an 'exact match', 65% of the scatterer locations are invariant 'within 1 pixel'. The cases labeled 'persistence' in Figure 2 enforce the constraint that the scatterer exist for the entire span of angles and very few scatterers continuously persist for even 5°. In the upper two cases (not labeled 'persistence') scintillation is allowed and the location invariance declines slowly with azimuth span. The 'within 1 pixel' results (which allow scintillation) are consistent with the one foot ISAR results of Dudgeon,² whose definition of persistence allowed scintillation. Because of the higher scatterer location invariance with 1° azimuth span, in our research we use 360 azimuth models for each target, in contrast to others who have used 5°, 10°, and 12 models.¹⁰
Figure 2. Scatterer location persistence, T72 #132.

The fact that the SAR scatterer locations do not persist over a span of even a few degrees, demonstrated in Figure 2, strongly indicates that observations at different azimuth angles are independent. Thus, what had previously been viewed as a "problem" for modeling, now presents a significant opportunity for integrating the results of SAR observations at multiple look angles.

3. SAR RECOGNITION SYSTEM

The SAR recognition system uses standard non-articulated models of the objects (at 1° azimuth increments) to recognize the same objects in non-standard, articulated and occluded configurations. The relative locations and magnitudes of the N strongest SAR scattering centers (local maxima in the radar return signal) are used as characteristic features. Using a technique like geometric hashing, the relative positions of pairs of scattering centers in the range (R) and cross-range (C) directions are the initial indices to a look-up table of labels that give the associated target type/pose and the remaining features: range and cross-range position of the 'origin' and the magnitudes of the two scatterers. (The 'origin', O, is the strongest of a pair of scatterers, the other is a 'point', P.) Any local reference point, such as a scattering center location, can be chosen as an origin to establish a reference coordinate system for building a model of an object at a specific azimuth angle pose. For ideal data, picking the location of the strongest scattering center as the origin is sufficient. However, for potentially corrupted data where any scattering center could be spurious or missing (due to the effects of noise, target articulation, occlusion, non-standard target configurations, etc.), we use all N strongest scattering centers in turn as the origin to ensure that a valid local reference point is obtained. Thus, to handle articulation and occlusion, the size of the look-up table models (and also the number of relative distances that are considered in the test image during recognition) are increased from N to N(N-1)/2.

The recognition process is an efficient search for positive evidence, using relative locations of scattering centers to access the look-up table and generate votes for the appropriate object, azimuth, range and cross-range translation. Constraints are applied to limit the allowable percent difference in the magnitudes of the data and model scattering centers to ±L%. (The design parameters N and L are optimized, based on experiments, to produce the best forced recognition results). Given the MSTAR targets are 'centered' in the chips, a ±5 pixel limit on allowable translations is imposed for computational efficiency. To accommodate some uncertainty in the scattering center locations, the eight-neighbors of the nominal range and cross-range relative location are also probed and the translation results are accumulated for a 3x3 neighborhood in the translation space. The process is repeated with different scattering centers as reference points, providing multiple queries of the model database to handle spurious scatterers that arise due to articulation, occlusion or configuration differences. The recognition algorithm actually makes a total of 9N(N-1)/2 queries of the look-up table to accumulate evidence for the appropriate target type, azimuth angle and translation.

To handle identification with 'unknown' objects, we introduce a criteria for the quality of the recognition result (e.g., the votes for the potential winning object exceed some threshold, D). By varying the decision rule parameter (typically from 50 to 400 votes in 10 vote increments) we obtain a form of Receiver Operating Characteristic (ROC) curve with probability of correct recognition (PCR) vs. probability of false alarm (PFA).
More formally, a radar image of object $c$ at azimuth $a$ consists of $N$ (or more) scatterers, each scatterer $k$ with a magnitude $S_k$ and range and cross-range locations $R_k$ and $C_k$, which (for consistency) are ordered by decreasing magnitude such that $S_k \geq S_{k+1}$ where $k = 1, \ldots, N$. A model $M$ of object $c$ at azimuth $a$ is given by:

$$M(c,a) = \{V_1(c,a), V_2(c,a), \ldots, V_{N(N-1)/2}(c,a)\}$$

(1)

which is comprised of the set of all pairwise observations, $V_i$:

$$V_i(c,a) = \{f_1, f_2, \ldots, f_6\}_i$$

(2)

where $i = 1, 2, \ldots, N(N-1)/2$, $f_1 = R_P - R_O$, $f_2 = C_P - C_O$, $f_3 = R_O$, $f_4 = C_O$, $f_5 = S_O$, $f_6 = S_P$, and with the individual scatterers in each pair labeled $O$ and $P$ so that $S_O \geq S_P$ for consistency (see Figure 3).

We define a match, $H$, as:

$$H(V_i, V_j) = \begin{cases} 1 & \text{if } |(f_b)_i - (f_b)_j| \leq \delta_b, \forall b = 1, \ldots, 6 \\ 0 & \text{otherwise} \end{cases}$$

(3)

where the match constraints are $\delta_1 = \delta_2 = 0$ pixels, $\delta_3 = \delta_4 = 5$ pixels and $\delta_5 = \delta_6 = L$ percent. A subscript $t$ applied to a match denotes that the match, $H_t$, is associated with the relative translation $t(R, C) = (\Delta f_3, \Delta f_4)$ of the stronger scatterers in the two observations.

The recognition result, $T$, for some test image (with a test class, $x$, and test azimuth, $y$, to be determined) is a maximal match that is greater than a threshold, $D$, given by:

$$T = \begin{cases} \{[c, a]\}, & \text{if } \max_{c,a,t} \left( \sum_{l=1}^{9} \sum_{k=1}^{N(N-1)/2} \sum_{m=1}^{9} H_l(V_k^n(x,y), V_m(c,a)) \right) > D \\ \text{"unknown"}, & \text{otherwise} \end{cases}$$

(4)

where $V_m \in M(c,a) \forall m$ such that $|\langle f_1 \rangle V_k^n - \langle f_1 \rangle V_m| = 0$ and $|\langle f_2 \rangle V_k^n - \langle f_2 \rangle V_m| = 0$ (note: this formulation avoids exhaustive search of all the models and can be implemented as a look-up table). The 9 observations (denoted by the superscript $n$ in $V_k^n$) are made to account for location uncertainty by taking the 3x3 neighbors about the nominal values for the relative locations $f_1$ and $f_2$ of scatterer pair $k$ in the test image. Similarly, the 9 matches (denoted by the superscript $l$ in $H_l$) are computed at the 3x3 neighbors located $\pm 1$ pixel about the resulting nominal value for translation, $t(R, C)$, of the scatterers in the test image from the model.
4. INDEPENDENCE OF MULTIPLE LOOK ANGLE SAR RECOGNIZERS

The azimuthal variance of SAR scatterer locations, previously demonstrated in Figure 2, strongly indicates that observations at different azimuth angles are independent. Given the probability of one SAR recognizer failing, $F_1$, where $F_1 = 1 - P_{CR}$; then if two recognizers are independent, the probability that both recognizers are wrong, $F_2$, is simply $F_2 = F_1^2$. In order to obtain the most failures, we pick the object configuration variant case, which we had previously determined\(^1\) to be the most difficult case for our SAR recognition approach (compared to the depression angle change and object articulation cases).

In the configuration variant experiments a single configuration of the T72 (#132) and BMP2 (#C21) vehicles are used as the models and the test data are two other variants of each vehicle type (T72 #812, #87 and BMP2 #9563, #9566), all at 15° depression angle. These results are obtained using the optimum parameters of 38 scattering centers and a percent magnitude change of less than ±11%. Figure 4 shows the probability that two recognizers are both wrong for forced recognition of configuration variants as a function of the difference in azimuth angle of the object from the two recognizers. (While Figure 4 emphasizes the small angles by only showing up to ±60 degrees, the results out to ±180 degrees are similar.) The single recognizer result, 19 failures of 414 trials, is an F1 failure rate of 0.0459, which is plotted for reference as point ‘a’ in Figure 4. For an F1 of 0.0459 the predicted value of F2 is 0.0021, which is very close to the overall experimental average F2 of 0.0025. The other interesting observation from Figure 4 is that the results are independent of the angle difference, even for very small values like 1 degree. This demonstration that multiple look angle SAR recognition results are independent, even for small angles down to 1 degree, provides the scientific basis for both measuring and improving the quality of recognition results.

5. MULTIPLE LOOK ANGLE SAR RECOGNITION RESULTS

5.1. Configuration Variants

In contrast to the forced recognition case described in the previous section, in these configuration variant experiments the BTR70 armored personnel carrier (#c71) is used as an unmodeled confuser vehicle to test the recognition system and the vote threshold parameter is used to generate “unknown” results. The other test conditions and parameters are the same as the forced recognition case (most significantly, the models are one configuration of the T72 and BMP2 vehicles and the test vehicles are two different configurations).

Figure 5 shows the effect of multiple look angle recognizers on the probability of false alarm using the BTR70 as a confuser. (The BTR70 is a more difficult case than other confusers such as the BRDM2 armored personnel carrier or the ZSU 23/4 anti-aircraft gun.)\(^1\) In the cases with two recognizers, the decision rule is that if either gives results above the vote threshold, the result is declared a target (which, for these BTR70 confusers, would be a false alarm). Thus, with this “target bias” decision rule the multiple recognizer cases have higher false alarms than a single recognizer. It is important to note that the penalty in increased false alarms is small for the left tail of the curve. Figure 5 also shows that the false alarm rates are similar for all the two look angle recognizer cases and that agreement on the “target” is basically irrelevant for a false alarm.
Figure 5. Effect of multi-look on probability of false alarm.

Figure 6. Effect of multi-look on probability of correct recognition.

Figure 6 shows the effect of multiple look angle recognizers on the probability of correct recognition for the configuration variant case where the test data are different configurations of the T72 and BMP2. The top curve shows the results for the 91.7 percent of the time when two recognizers at different look angles agree on the result. The bottom curve is for the remaining 8.3 percent of the time when the two recognizers disagree and the answer that gets the most votes is chosen. The second curve, labeled “best of two”, uses a decision level fusion rule that simply picks the target based on which of the two recognizers got the most votes. (This case is also the weighted average of the agree and disagree cases). In Figure 6 the probability of correct recognition decreases as the vote threshold increases (to the left in Figure 6), because the higher threshold causes more targets to be classified as “unknown.” The recognition results for using the best of two recognizers at different look angles are substantially better than the results for a single recognizer. This is basically the result of fewer “misses”, where a target object is classified as an “unknown”; because there are two opportunities to get above the vote threshold and declare a “target.”

Figure 7 combines the results of Figures 5 and 6 and shows the effect of using multiple look angle recognizers on the Receiver Operating Characteristic curve for the configuration variant cases. These recognition results, using the best of two recognizers at different look angles, are substantially better than the results for a single recognizer. For example, at a 0.10 PFA the PCR for the best of two look angles is 0.8324, compared to 0.7091 for a single recognizer. The performance improvement is because the cost in increased false alarms (in Figure 5) is low compared to the benefits in increased recognition (in Figures 6), due to fewer targets being classified as “unknown”.

5.2. Articulation and Occlusion

In the articulated object experiments the models are non-articulated versions of T72 tank #a64 and ZSU 23/4 anti-aircraft gun #d08 (with the gun turret straight forward) and the test data are articulated versions of these same
serial number objects (with the turret rotated) and BRDM2 armored personnel carrier #e71 as a confuser vehicle (all at 30° depression angle). The results of applying the same techniques (and all the same recognition system parameters) in these articulated object experiments are shown as ROC curves in Figure 8. Again the results for using two recognizers at different look angles and picking the answer with the largest number of votes are better than the single recognizer results.

The occlusion experiments use four models: T72 tank #132, BMP2 APC #C21, BTR70 APC #c71 and ZSU23/4 gun #d08 and the unmodeled confuser vehicle is BRDM2 APC (#e71) (all at 15° depression angle). Since there is no real SAR data with occluded objects available to the general public, the occluded test data in this paper is simulated by starting with a given number of the strongest scattering centers in target chips of these same four objects and then removing the appropriate number of scattering centers encountered in order from one of four perpendicular directions $d_i$ (where $d_1$ and $d_3$ are the cross range directions, along and opposite the flight path respectively, and $d_2$ and $d_4$ are the up range and down range directions). Then the same number of scattering centers (with random magnitudes) are added back at random locations within the original bounding box of the chip. This is the same technique used in$^4$; it keeps the number of scatterers constant and acts as a surrogate for some potential occluding object. In some of our previous work on occluded objects,$^4$ the confuser vehicle was occluded. However, while the target may be occluded, the confuser vehicle may not necessarily be occluded in the practical case. Hence, in this research the BRDM2 APC (#e71) is an unoccluded confuser vehicle, which is a substantially more difficult case.

Figure 9 shows the effect of multiple look angle recognizers on the probability of correct recognition for the case of 50% occluded targets and an unoccluded confuser. The same techniques (and all the same recognition system parameters) used in the prior configuration variant and articulation experiments are applied to these occluded object

---

Figure 7. Effect of multi-look on configuration variant ROC curve.

Figure 8. Effect of multi-look on articulated object ROC curve.
experiments. Here again, using two recognizers at different look angles and a decision level fusion rule of picking the answer with the largest number of votes gives better results than a single recognizer.

6. CONCLUSIONS AND FUTURE WORK

The fundamental azimuthal variance of SAR scatterer locations can be successfully used as the basis for a principled and effective multiple look angle SAR recognition approach. The experiments demonstrate that SAR recognition results at different azimuths are independent, even for small azimuths, such as one degree. In addition, using decision level fusion of two observations at different look angles can substantially increase SAR recognition performance for target configuration variants. These techniques can also be successfully applied to recognition of articulated objects and occluded objects.

This paper considers only two look angles, but a similar approach could be used for more look angles. In addition, more formal methods, like Dempster-Shafer and Bayesian approaches, can be used for decision level fusion. Our approach can be applied to resolve ambiguities with multiple looks from the same or different sensor platforms.

ACKNOWLEDGMENTS

This work was supported by DARPA/AFOSR grant F49620-97-1-0184; the contents and information do not necessarily reflect the position or policy of the U.S. Government.

REFERENCES

